



Fun with 2D Glasses

and a Sprinkling of Special Relativity

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How to make “2D glasses”

- Take two pairs of 3D glasses.
- Cut them each in half.
- Join together halves of the same colour.
- The result is a pair of binocular colour filters, 1 for red, one for cyan.
- I call these “2D glasses” because if you view a 3D picture through them it will look flat.
- The same technique can be used with polarised glasses if you don't like watching films in 3D! (Cardboard frames required).

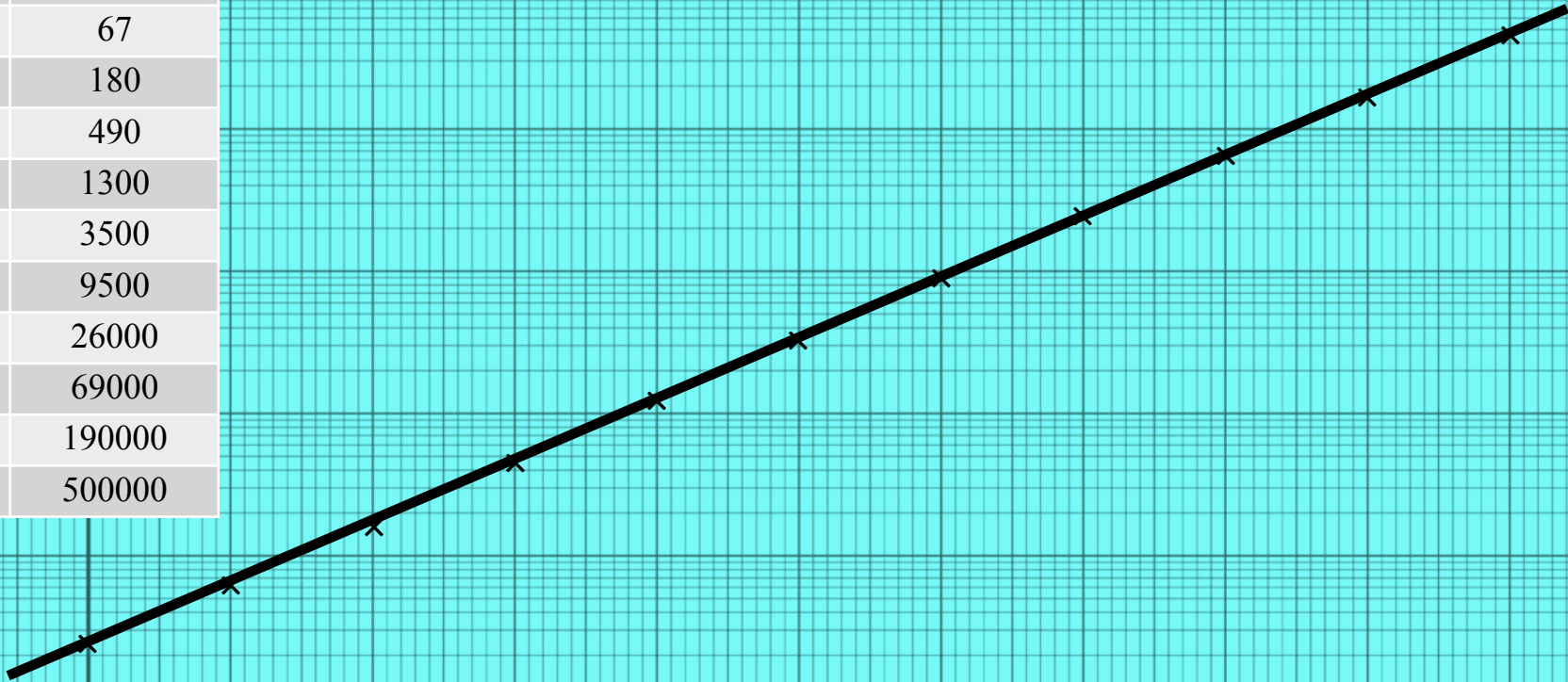
What you can do with them

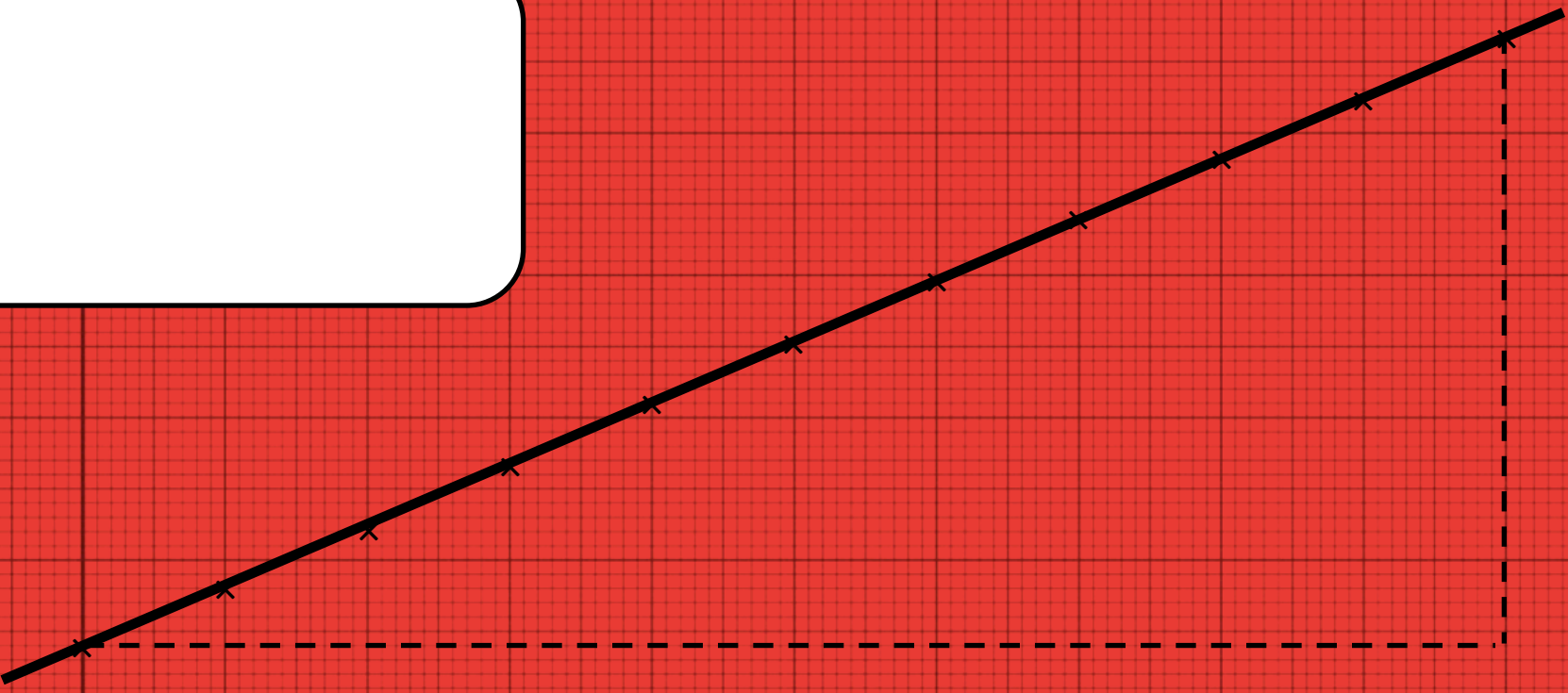
- Many situations can be understood better by viewing them from more than one point of view.
- 2D glasses allow you to overlay two different scales/coordinate systems, but see just one or the other at any one time.
- Any information displayed will be visible from both points of view, allowing easy translation between the two, and assurance of logical consistency.

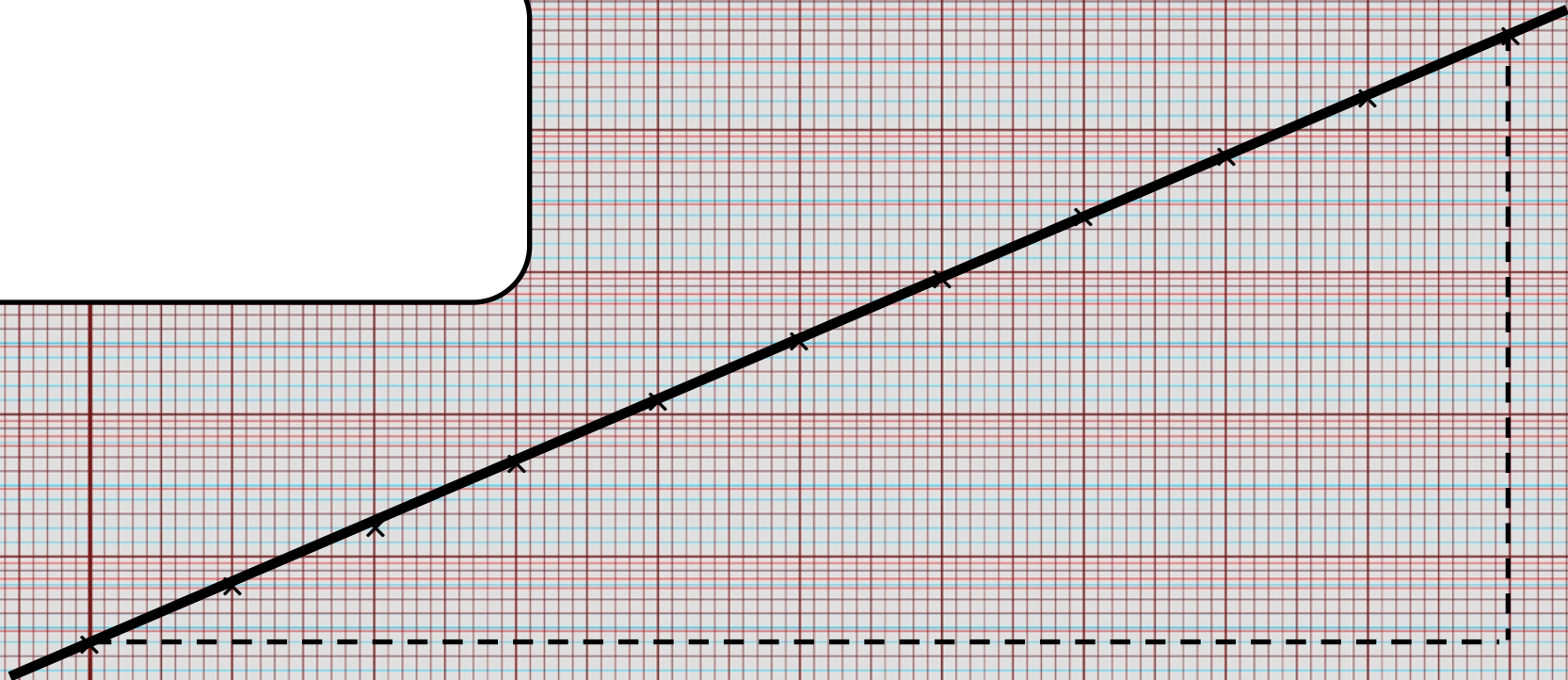
Example I: Exponential Variation

Test whether data fits the exponential form $y = ae^{bx}$ and establish the values of both a and b .

x	y
0	25
1	67
2	180
3	490
4	1300
5	3500
6	9500
7	26000
8	69000
9	190000
10	500000







Example II: Power Laws

Test whether data fits the .



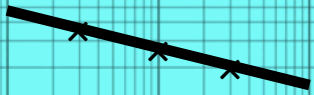
length $\approx 7 \times 300 \text{ km}$
 $\approx 2100 \text{ km}$



length $\approx 28 \times 100 \text{ km}$
 $\approx 2800 \text{ km}$



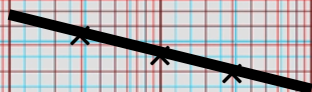
length $\approx 136 \times 30 \text{ km}$
 $\approx 3780 \text{ km}$





This corresponds to a fractional dimension of

$$d =$$

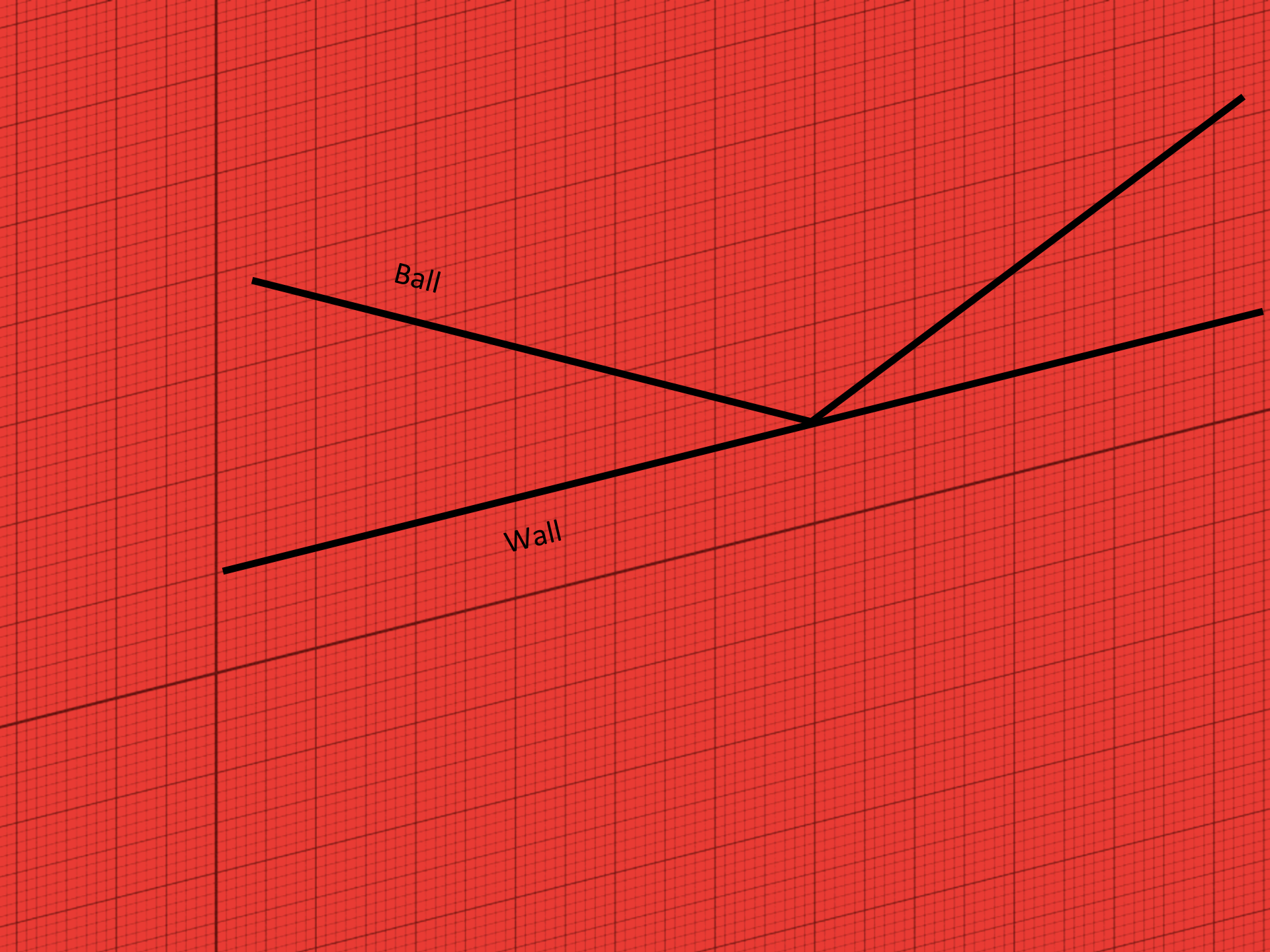


This corresponds to a fractional dimension of

$$d =$$

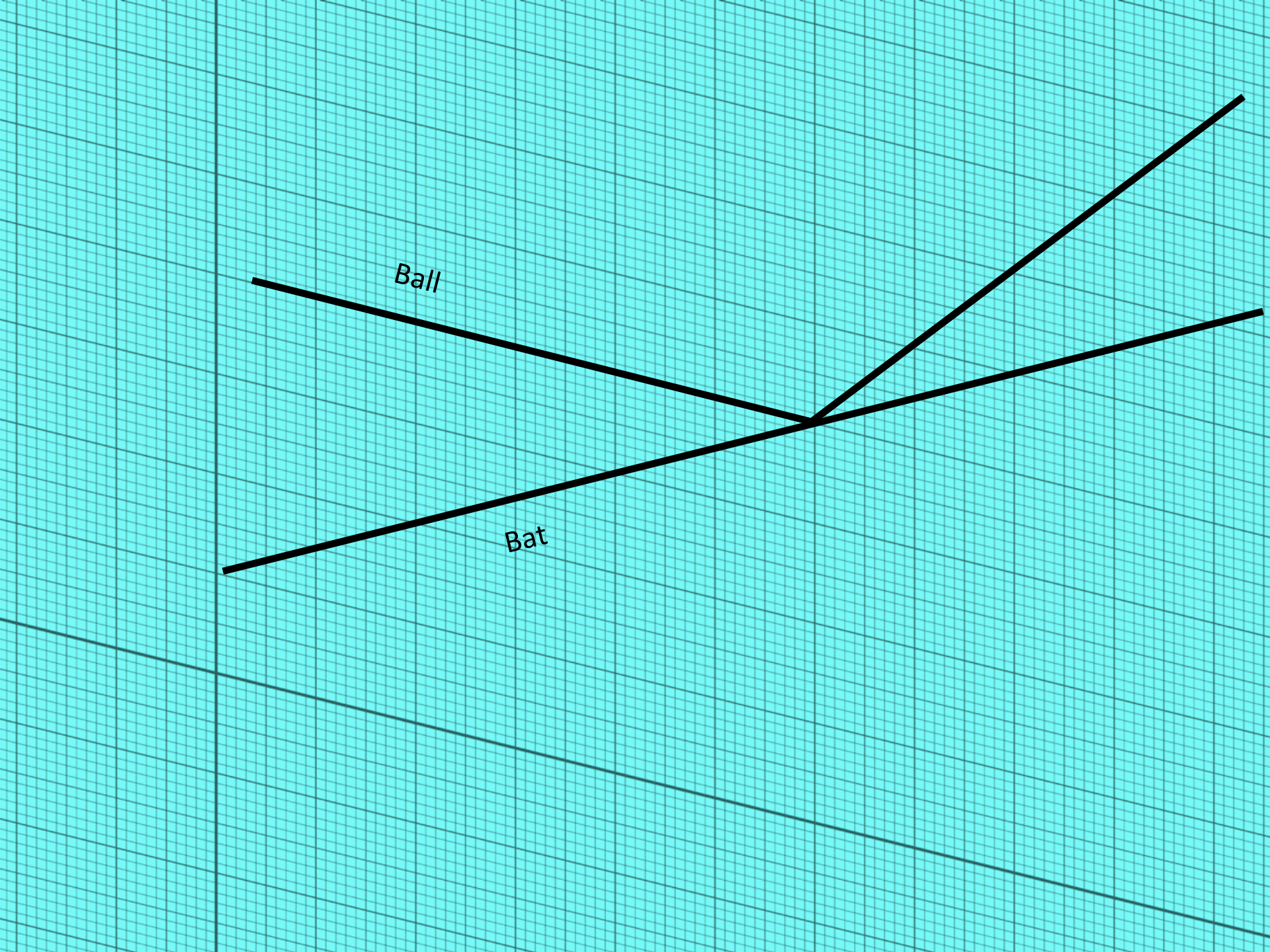
Example III: Galilean Relativity

- Galilean relativity is the principle that Newton's Laws apply in all inertial reference frames.
- Observers moving at different velocities will have different, but consistent, views of the universe.
- The link between the two views is described by the Galilean Transformation:



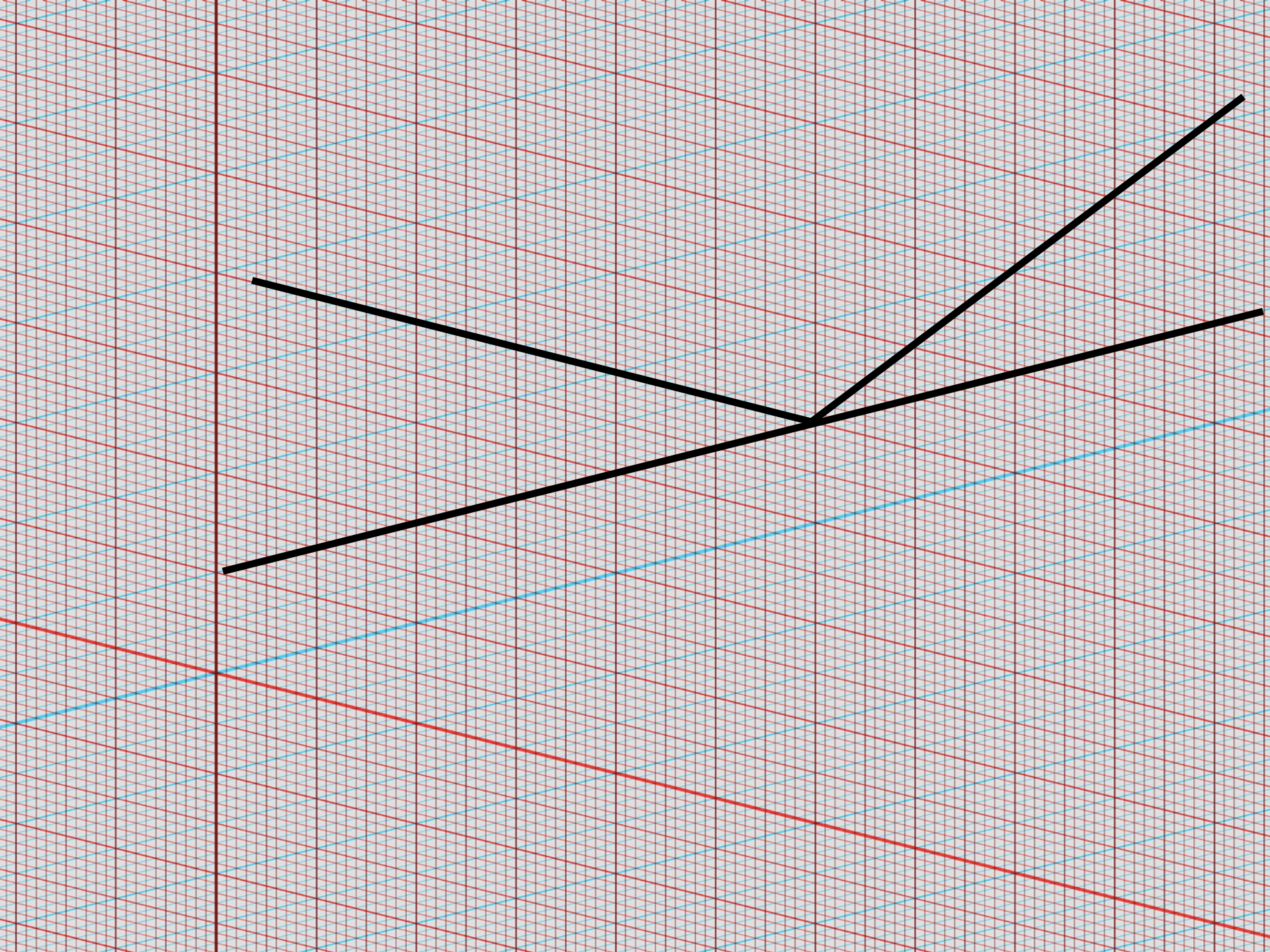
Ball

Wall



Ball

Bat

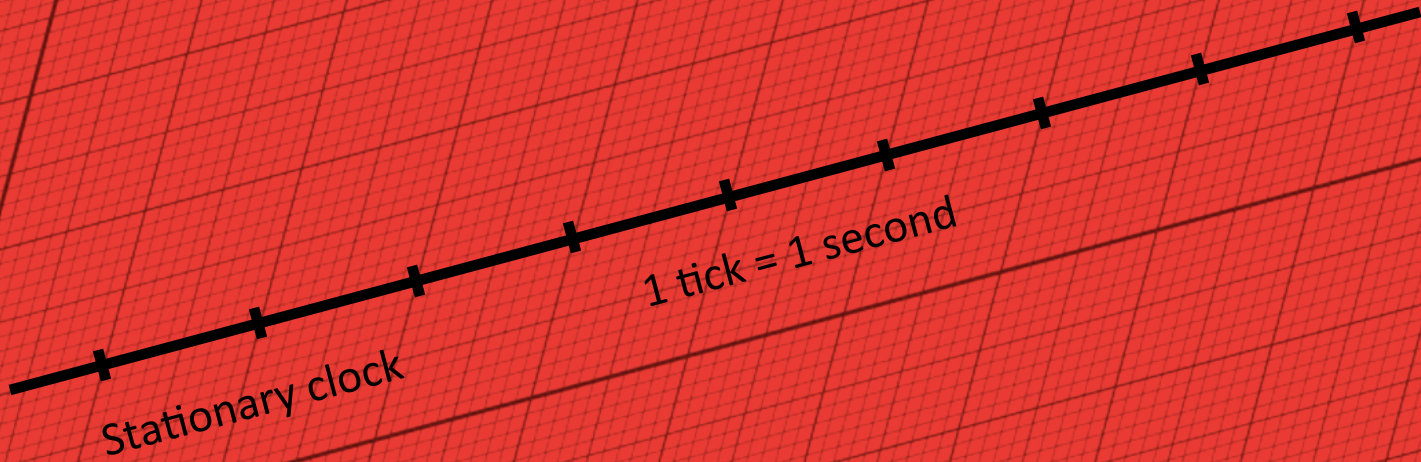


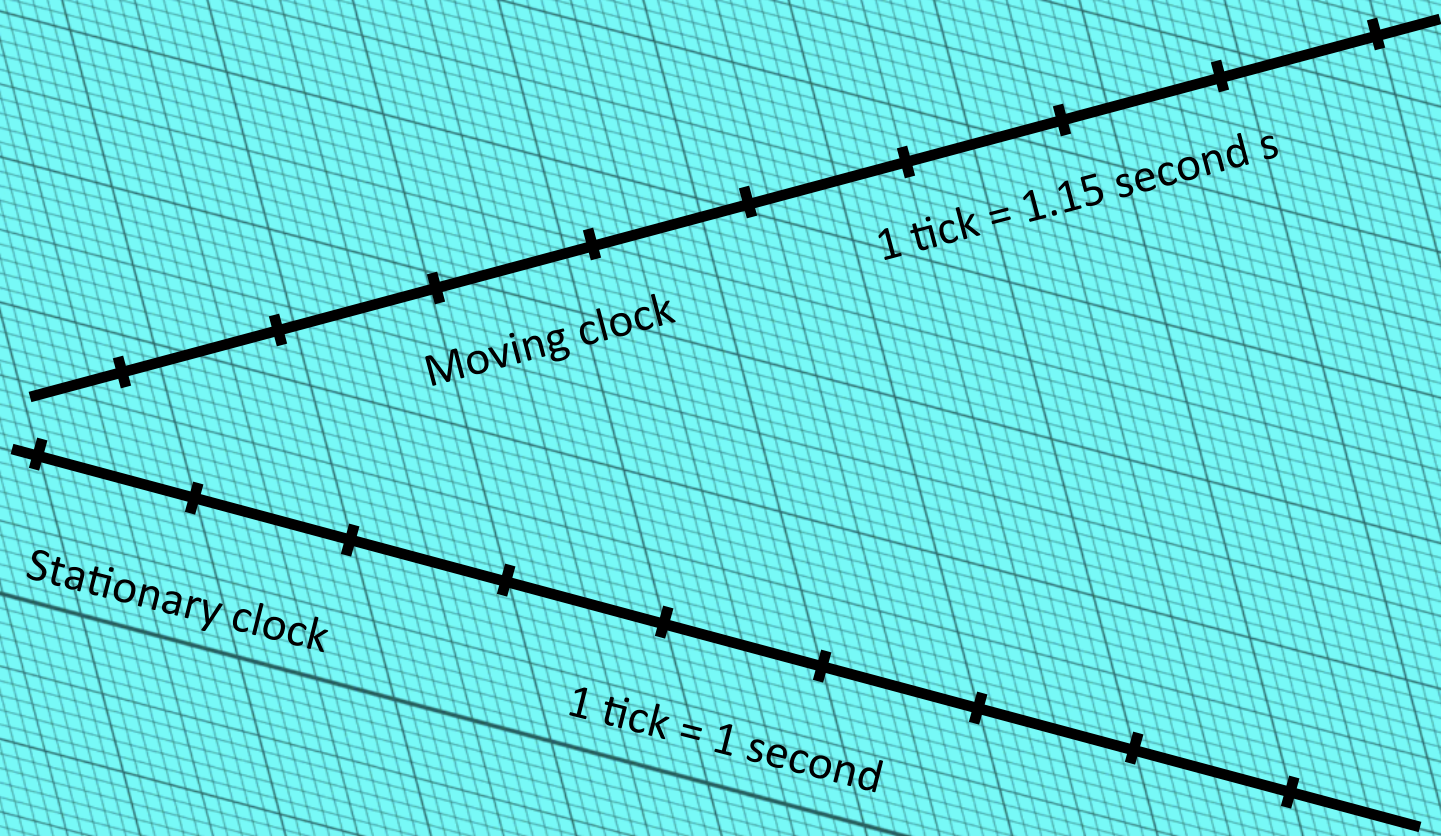
Example IV: Special Relativity

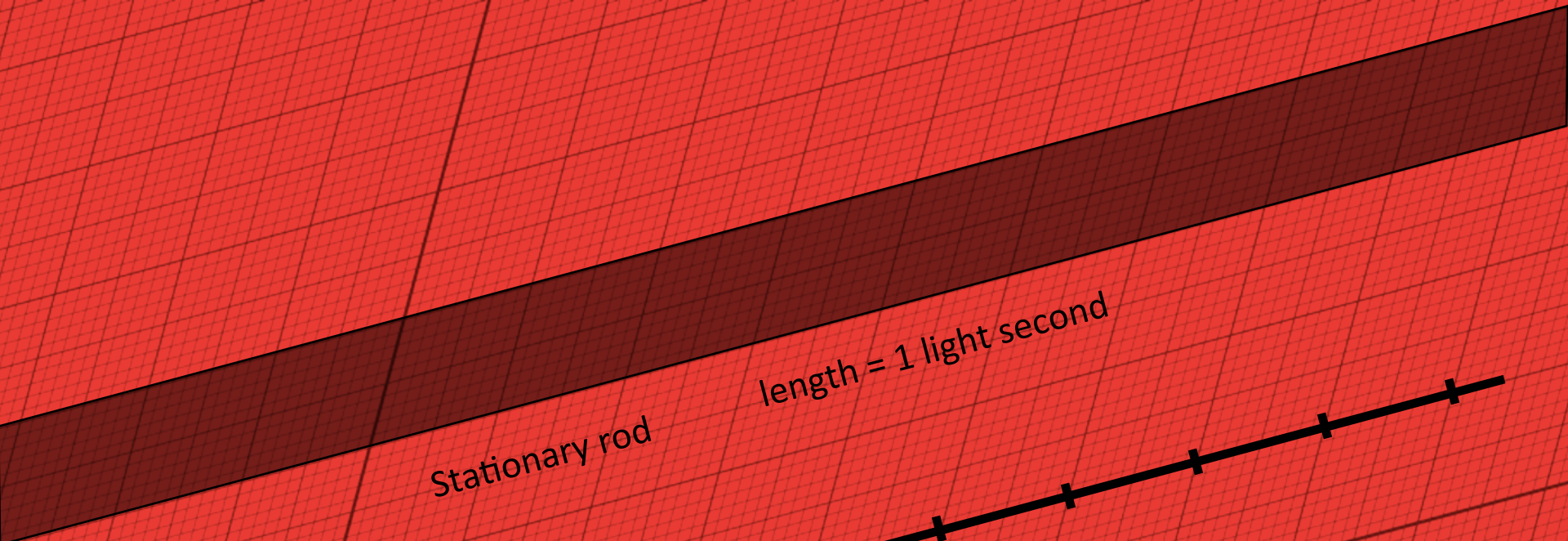
- Special relativity is the principle that the laws of physics apply in all inertial reference frames.
- Observers moving at different velocities will have different, but consistent, views of the universe.
- The link between the two views is described by the Lorentz Transformation:

where

- If $\beta = v/c$ then $\gamma = 1/\sqrt{1-\beta^2}$ and $\beta\gamma = \gamma v/c$.

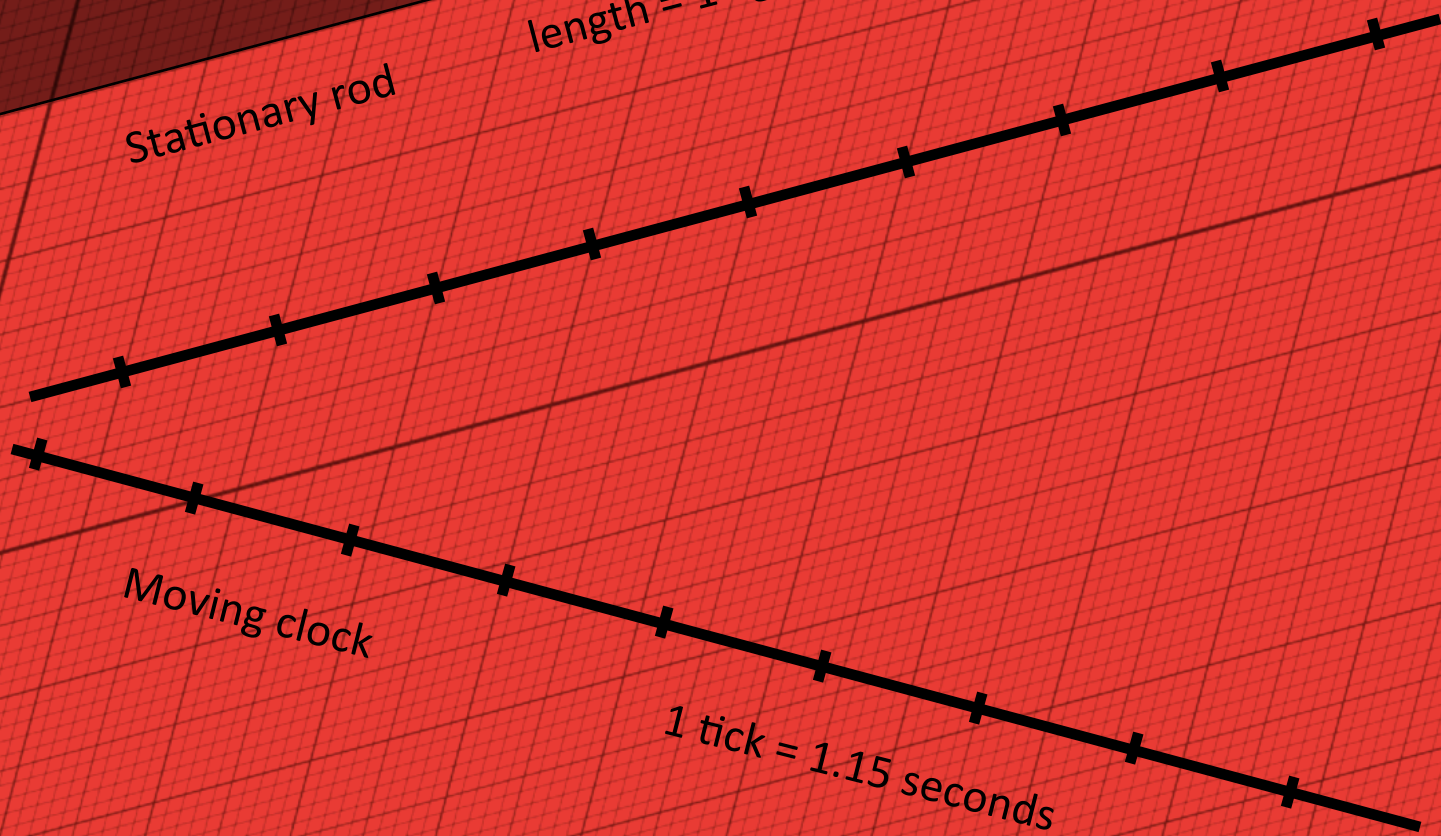






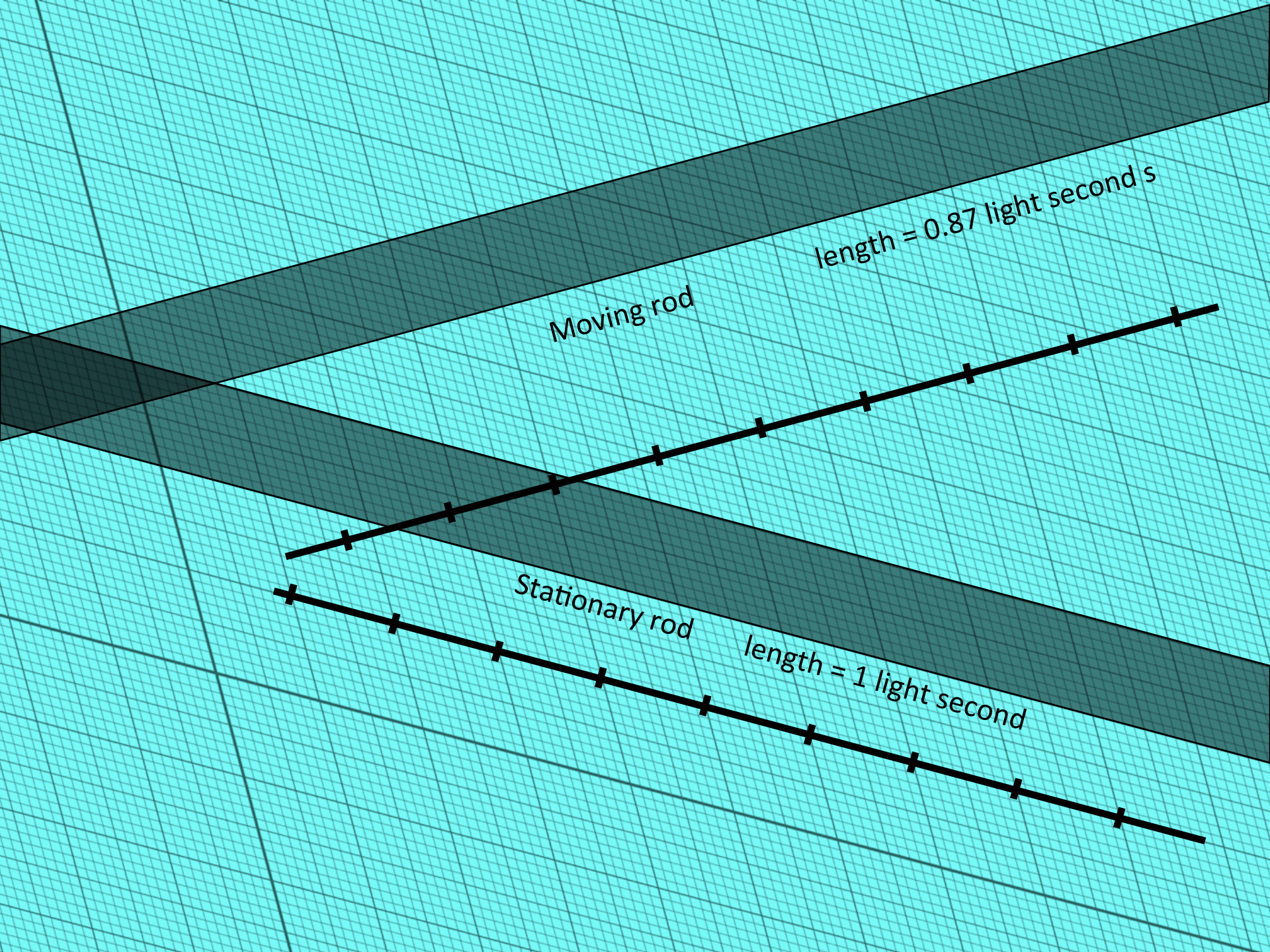
Stationary rod

length = 1 light second



Moving clock

1 tick = 1.15 seconds

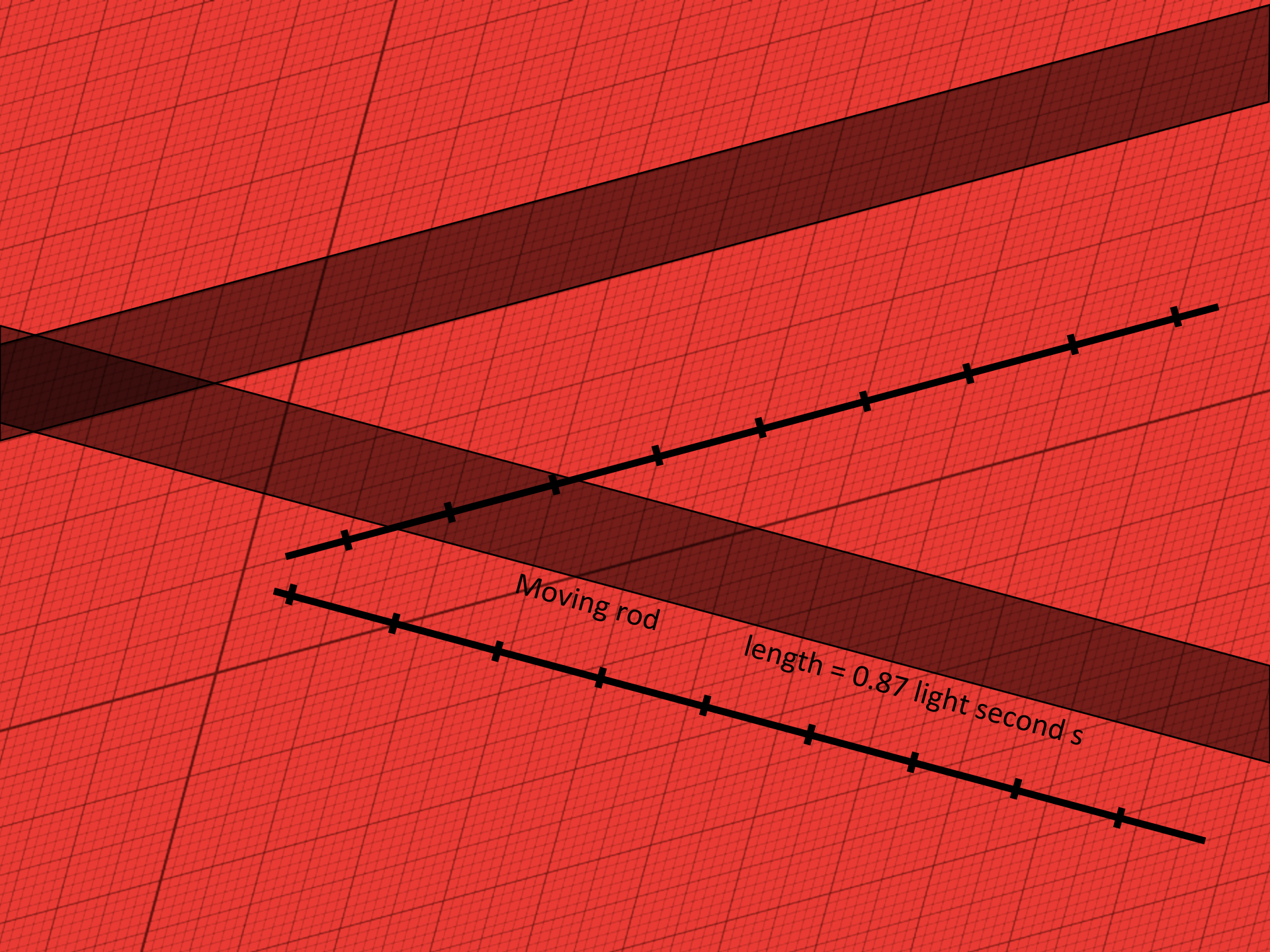


Moving rod

length = 0.87 light second s

Stationary rod

length = 1 light second



Moving rod

length = 0.87 light second s

